

COMSOL CONFERENCE

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Implementation of a Thermo- Hydrodynamic Model to Predict “Morton Effect”

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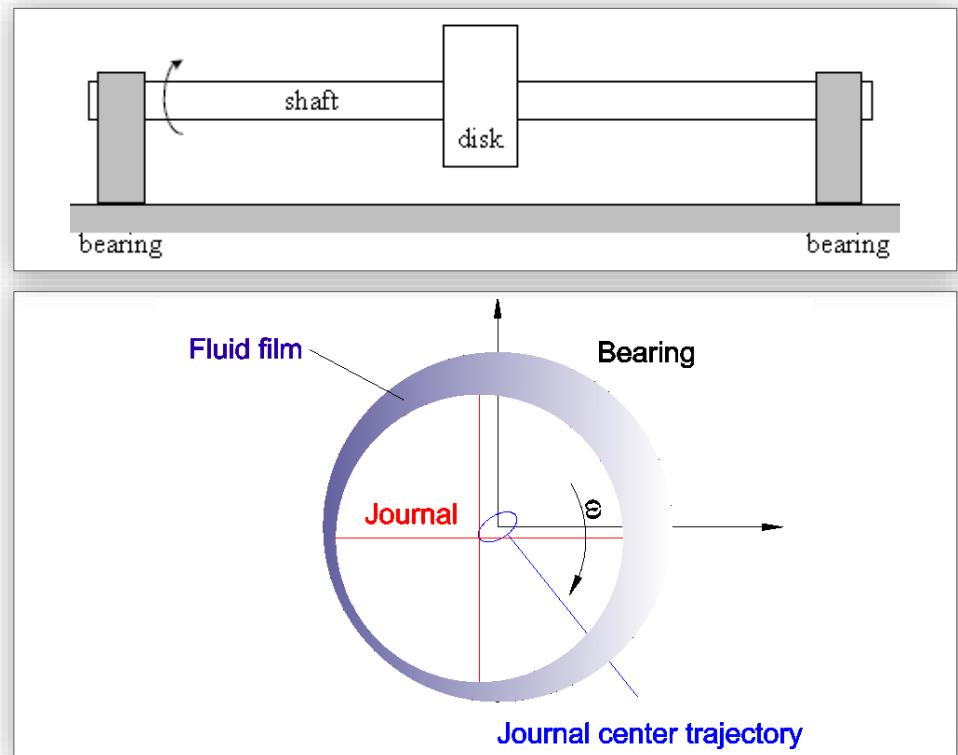
October 13th, 2016

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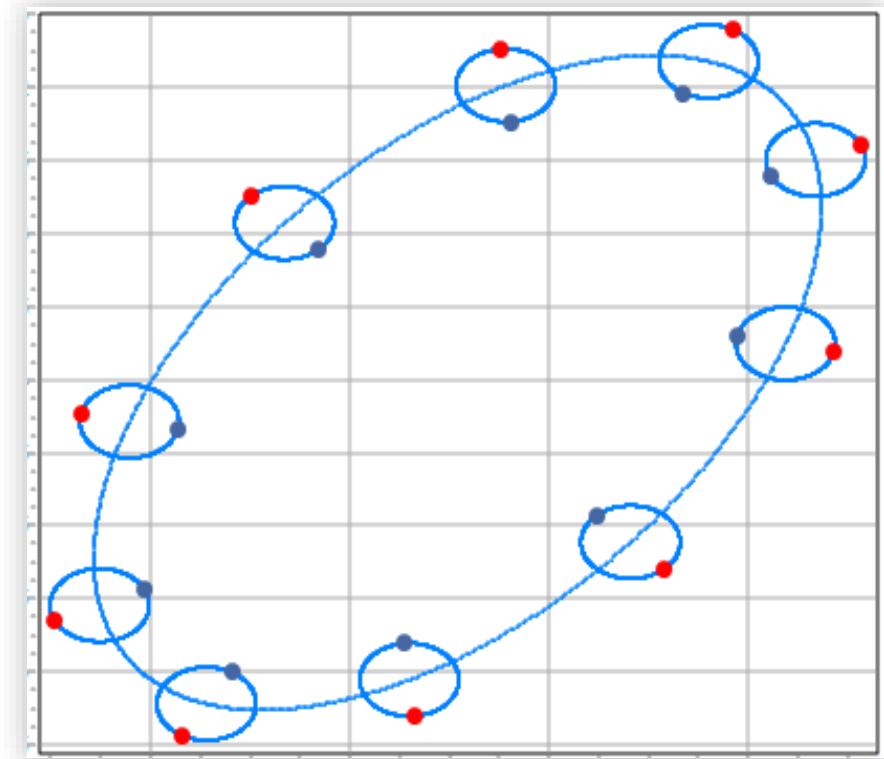
1.A - Morton effect and its explanations

- Shaft sustained with fluid film bearings
- Every journal has a residual unbalance
- The journal exhibits a synchronous orbit



1.B - Morton effect and its explanations

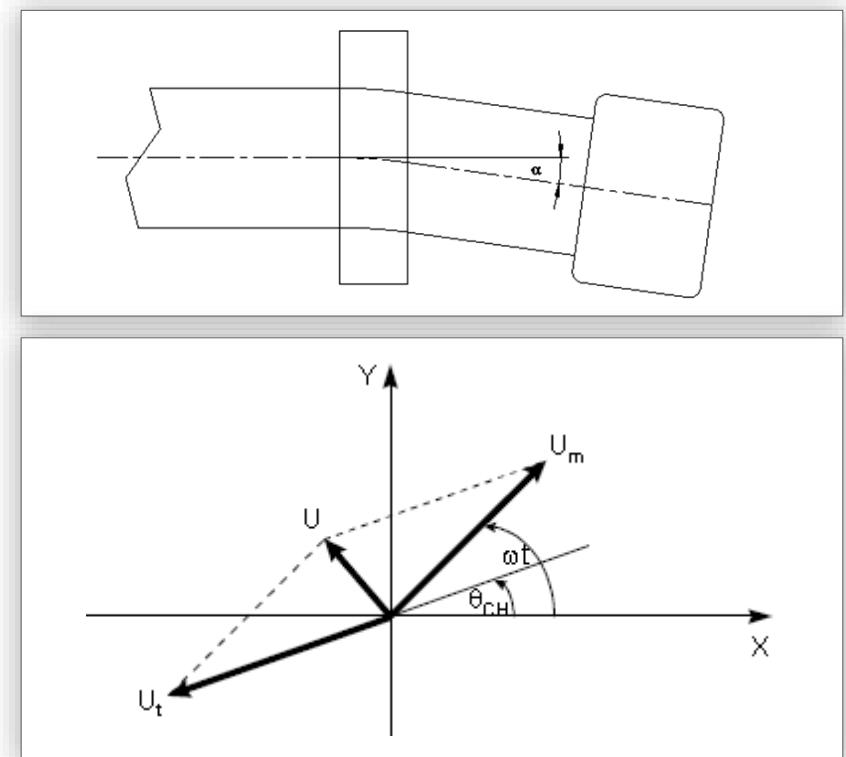
- Inside fluid film bearing a small part of the journal is HOT, while the opposite side is COLD
- Non uniform temperature distribution inside oil
- Thermal bending



1.C - Morton effect and its explanations

Now consider an overhung mass...

- Thermal bending causes a certain unbalance
- Thermal unbalance can:
 - ♦ reinforce the effect reducing again minimum film thickness (UNSTABLE)
 - ♦ reduce the effect counter-balancing the mechanical unbalance (STABLE)

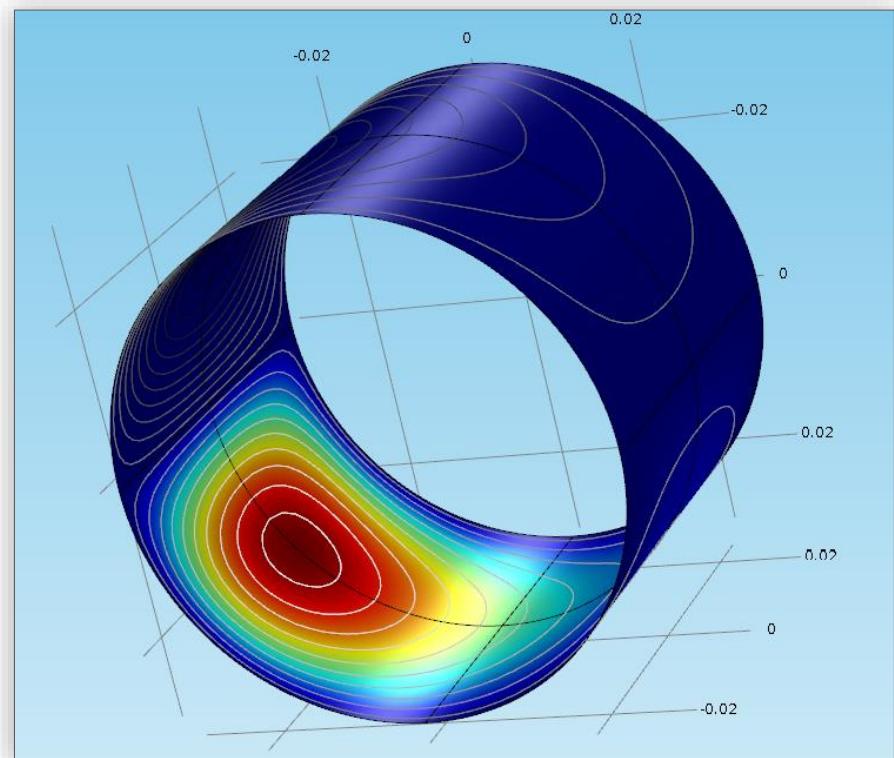


2.A - Physics behind the effect

CFD physics: Reynolds equation

$$\begin{cases} \nabla_T \cdot \left(\frac{-\rho h^3}{12\mu} \nabla_T p + \frac{\rho h}{2} (\nu_a + \nu_b) \right) = \frac{\partial(\rho h)}{\partial t} \\ p(x, y) = 0 \end{cases}$$

$(x, y) \in \Omega_1$
 $(x, y) \in \Omega_2$

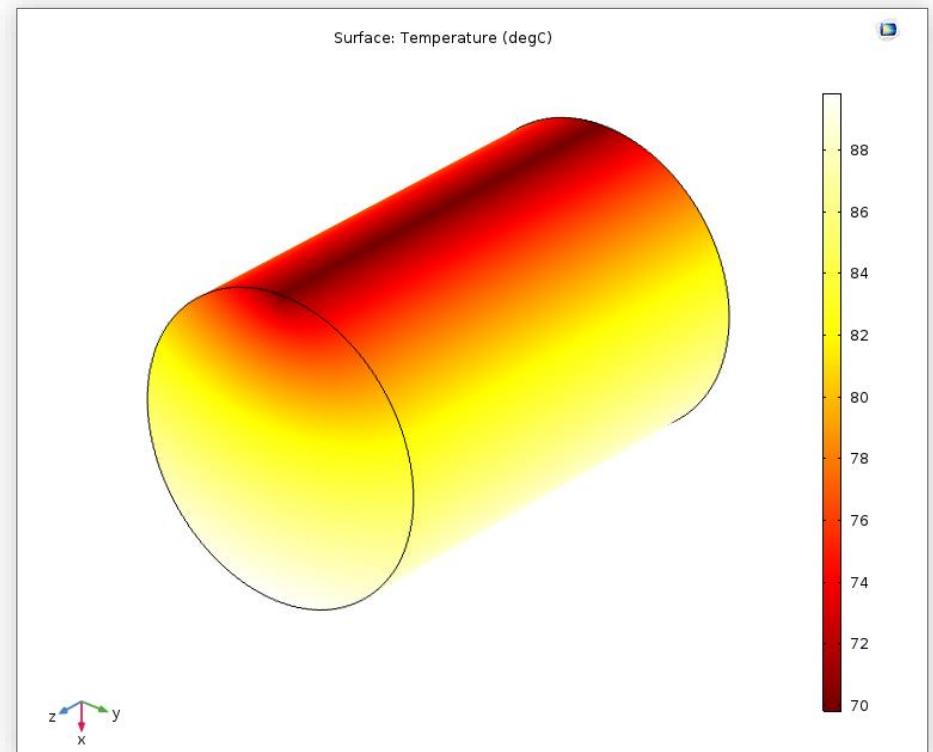


2.B - Physics behind the effect

Thermal physics

Energy generation rate + Influx energy rate
= energy accumulation rate

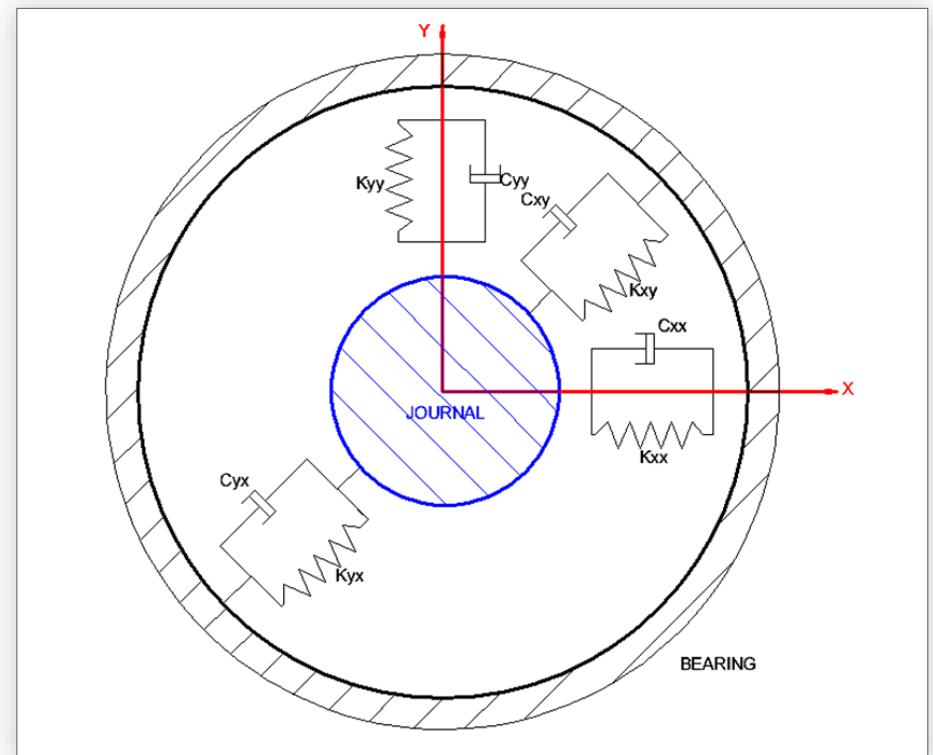
$$\dot{q} + \nabla \cdot (k \nabla u) = u_t$$



2.C - Physics behind the effect

Mechanical physics and
multibody dynamics

$$M\ddot{X} + C\dot{X} + KX = Mu\omega^2 \begin{pmatrix} \sin \omega t \\ \cos \omega t \end{pmatrix}$$



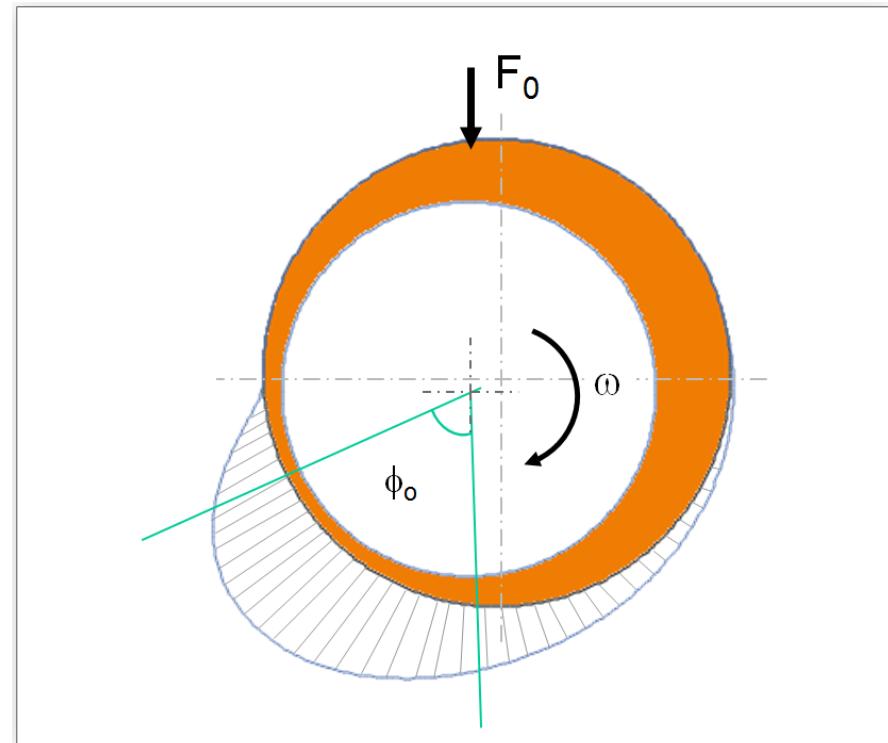
3.A - Approximation and methodology

**Static equilibrium position
(short bearing approximation)**

$$F_0 = \mu\omega RL \left(\frac{L}{C}\right)^2 \frac{\varepsilon \sqrt{16\varepsilon^2 + \pi^2(1-\varepsilon^2)}}{(1-\varepsilon^2)^2}$$

$$\tan(\phi_0) = \frac{\pi\sqrt{1-\varepsilon^2}}{4\varepsilon}$$

A. C. Balbahadur, R. G. Kirk, Part I—Theoretical Model for a Synchronous Thermal Instability Operating in Overhung Rotors, International Journal of Rotating Machinery, 10(6): 469–475, 2004



3.B - Approximation and methodology

Orbit and motion (short bearing approximation)

$$k_{xx} = K_{xx} \frac{C}{F_0} = \frac{f_{r0}}{\varepsilon(1-\varepsilon^2)} (f_{r0}^2 + 1 + 2\varepsilon^2)$$

$$k_{yy} = K_{yy} \frac{C}{F_0} = \frac{f_{r0}}{\varepsilon(1-\varepsilon^2)} (f_{t0}^2 + 1 - \varepsilon^2)$$

$$k_{yx} = K_{yx} \frac{C}{F_0} = \frac{f_{t0}}{\varepsilon(1-\varepsilon^2)} (f_{r0}^2 - 1 + \varepsilon^2)$$

$$k_{xy} = K_{xy} \frac{C}{F_0} = \frac{f_{t0}}{\varepsilon(1-\varepsilon^2)} (f_{r0}^2 + 1 + 2\varepsilon^2)$$

$$c_{xx} = C_{xx} \frac{C\omega}{F_0} \frac{2f_{t0}}{\varepsilon(1-\varepsilon^2)} ((2+\varepsilon^2)f_{r0}^2 + 1 - \varepsilon^2)$$

$$c_{yy} = C_{yy} \frac{C\omega}{F_0} = \frac{2f_{t0}}{\varepsilon(1-\varepsilon^2)} ((2+\varepsilon^2)f_{t0}^2 - 1 + \varepsilon^2)$$

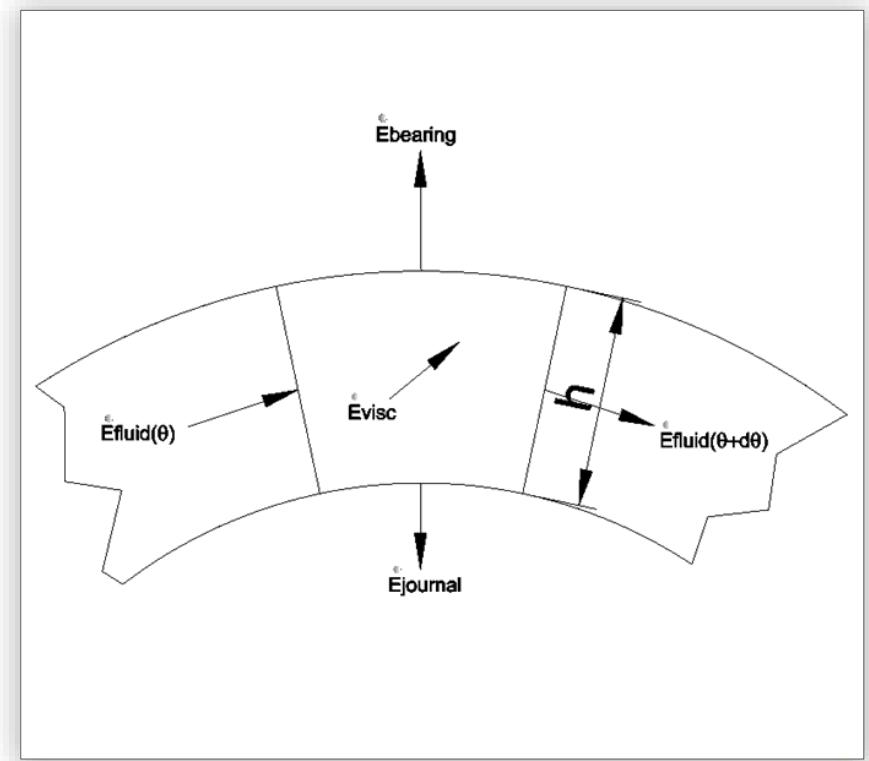
$$\begin{aligned} c_{xy} &= c_{yx} = C_{xy} \frac{C\omega}{F_0} = \\ &= \frac{2f_{r0}}{\varepsilon(1-\varepsilon^2)} ((2+\varepsilon^2)f_{t0}^2 - 1 + \varepsilon^2) \end{aligned}$$

3.C - Approximation and methodology

**Temperature distribution
(short bearing approximation)**

$$\dot{E}_{visc} = \dot{E}_{fluid}(\vartheta + d\vartheta) - \dot{E}_{fluid}(\vartheta) + \dot{E}_{journal} + \dot{E}_{bearing}$$

$$\frac{dT}{d\xi} + \frac{2H}{\rho c \omega h} - \left(\frac{2HT_{amb}}{\rho c \omega h} + \frac{2\mu \omega R_j^2}{\rho ch^2} \right) = 0$$

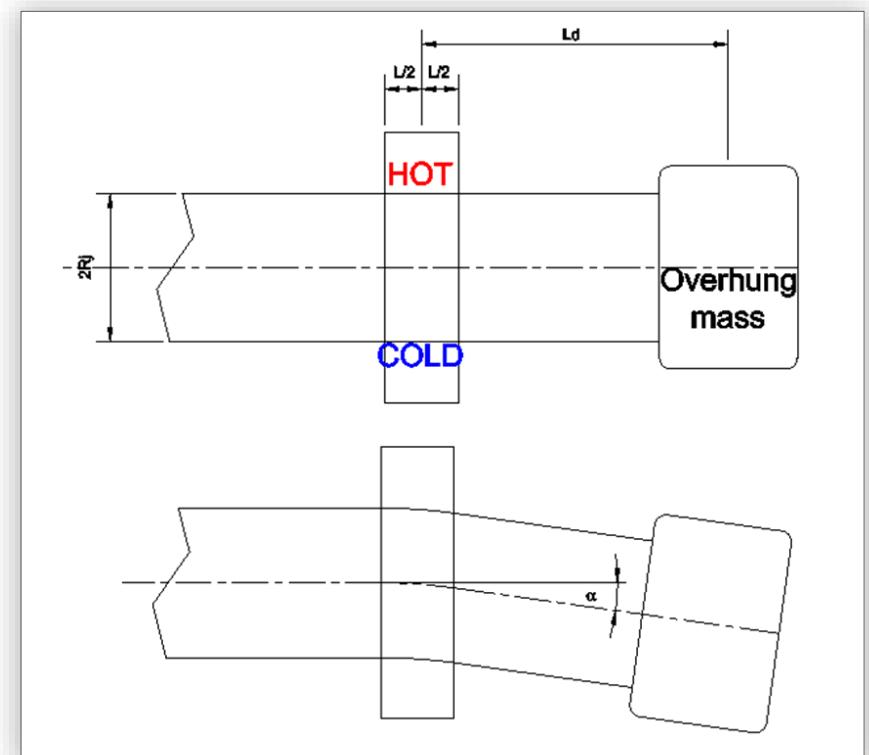


3.D - Approximation and methodology

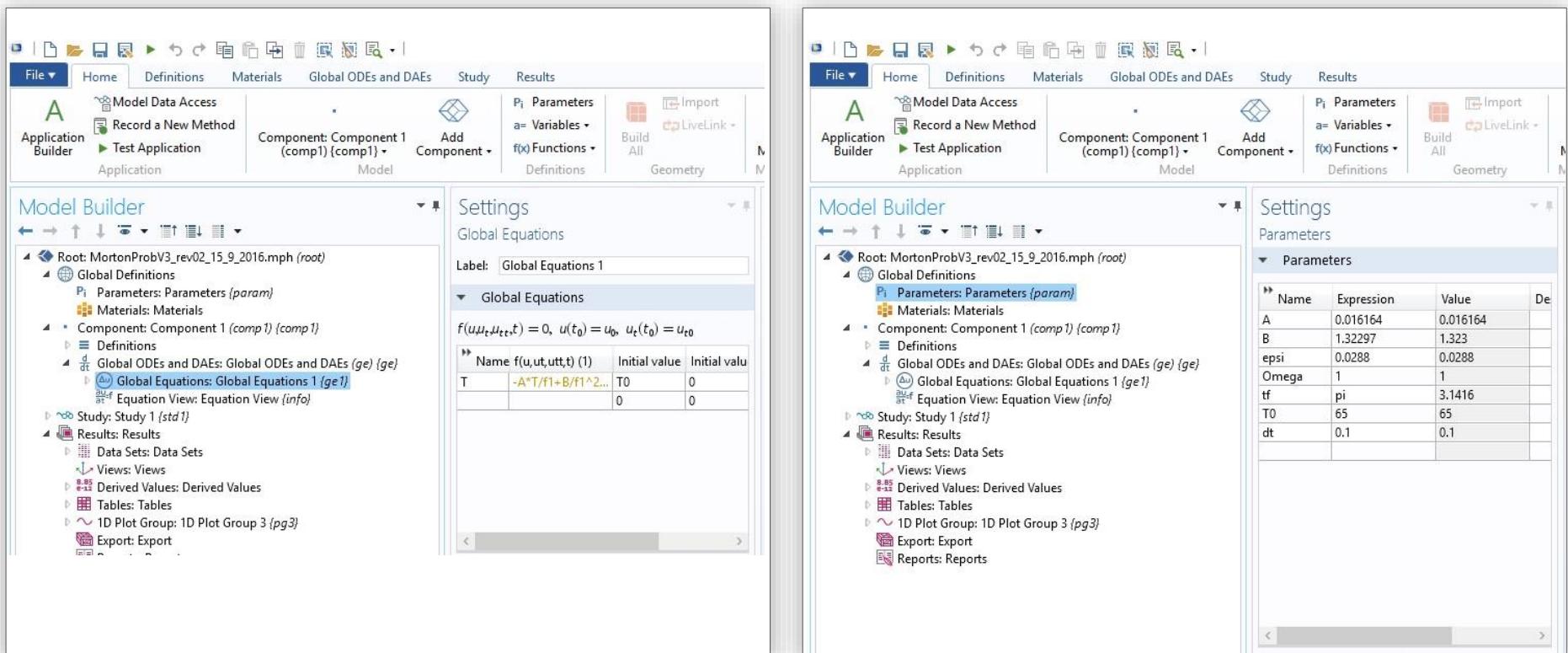
Unbalance (mechanical, total, limit)

$$U_t = m_o y_o = m_o \frac{\alpha \Delta T}{R_j} L L_o$$

$$U_{thr} = \frac{0.15 \text{ W}}{\omega^2}$$



4 – Comsol implementation



The image displays two side-by-side screenshots of the Comsol Model Builder interface, illustrating the setup of a numerical model.

Left Screenshot (Model Builder - Global Equations):

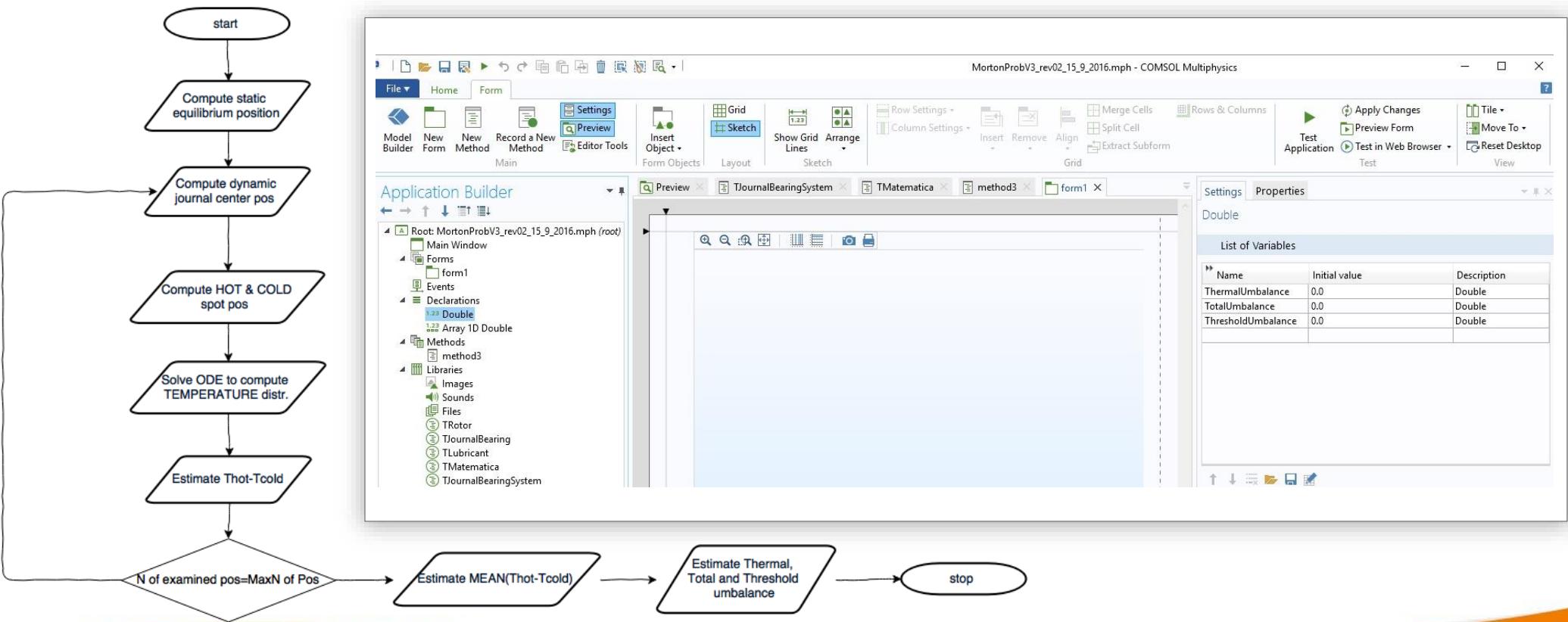
- Toolbar:** File, Home, Definitions, Materials, Global ODEs and DAEs, Study, Results.
- Application Bar:** Model Data Access, Record a New Method, Component: Component 1 (comp1) {comp1}, Add Component, Parameters, Import, LiveLink, Build All, Definitions, Geometry.
- Model Builder Tree:**
 - Root: MortonProbV3_rev02_15_9_2016.mph (root)
 - Global Definitions
 - Parameters: Parameters {param}
 - Materials: Materials
 - Component: Component 1 (comp1) {comp1}
 - Definitions
 - Global ODEs and DAEs: Global ODEs and DAEs (ge) {ge}
 - Global Equations: Global Equations 1 (ge1)
 - Equation View: Equation View {info}
 - Study: Study 1 (std1)
 - Results: Results
 - Data Sets: Data Sets
 - Views: Views
 - Derived Values: Derived Values
 - Tables: Tables
 - 1D Plot Group: 1D Plot Group 3 (pg3)
 - Export: Export
- Settings Panel:**

Global Equations

Label: Global Equations 1

Name	Initial value	Initial value
f(u,u_t,u_tt,t)	-A*T/f1+B/f1^2...	T0
	0	0

4 – Comsol implementation





4 – Comsol implementation

The screenshot shows the Comsol Application Builder interface. The top menu bar includes File, Home, Method, Settings, Preview, Editor Tools, Utility Class, Java External Java Library, External C Library, Language Elements, Model Expressions, Check Syntax, Go to Node, Record Code, Extract Variable, Continue, Step, Step Into, Stop, Debug Log, and Remove All. The main window has tabs for Preview, TJournalBearingSystem, TMatematica, method3, and form1. The left sidebar shows the application structure: Root MortonProbV3_rev02_15_9_2016.mph (root) containing Main Window, Forms (form1), Events, Declarations (1.2 Double, 1.23 Array 1D Double), Methods (method3), and Libraries (Images, Sounds, Files, TRotor, TJournalBearing, TLubricant, TMatematica, TJournalBearingSystem). The code editor on the right contains the following M-script:

```
//dynamic cold spot position
xc = xj+FJournalBearing.JournalRadius*Math.cos(FRotor.Speed*t+g0+Math.PI);
yc = yj+FJournalBearing.JournalRadius*Math.sin(FRotor.Speed*t+g0+Math.PI);
thc = Math.atan2(yc, xc);
xic = TMatematica.mppi(Math.PI-(FRotor.Speed*t+g0+Math.PI-thj));

//solve differential equation for temperature distribution around journal circumference

FEps2 = Math.sqrt(TMatematica.sqr(xj)+TMatematica.sqr(yj))/FJournalBearing.RadialClarence;

model.param().set("epsi", FEps2);
model.study("std1").run();
useGraphics(model.result("pg3"), "graphics1");

if (i2 == 1) {
    model.result().table("tbl1").clearTableData();
    with(model.result().numerical("gev1"));
        set("table", "tbl1");
    endwith();
    model.result().numerical("gev1"). setResult();
}
else {
    with(model.result().numerical("gev1"));
        set("table", "tbl1");
    endwith();
    model.result().numerical("gev1").appendResult();
}

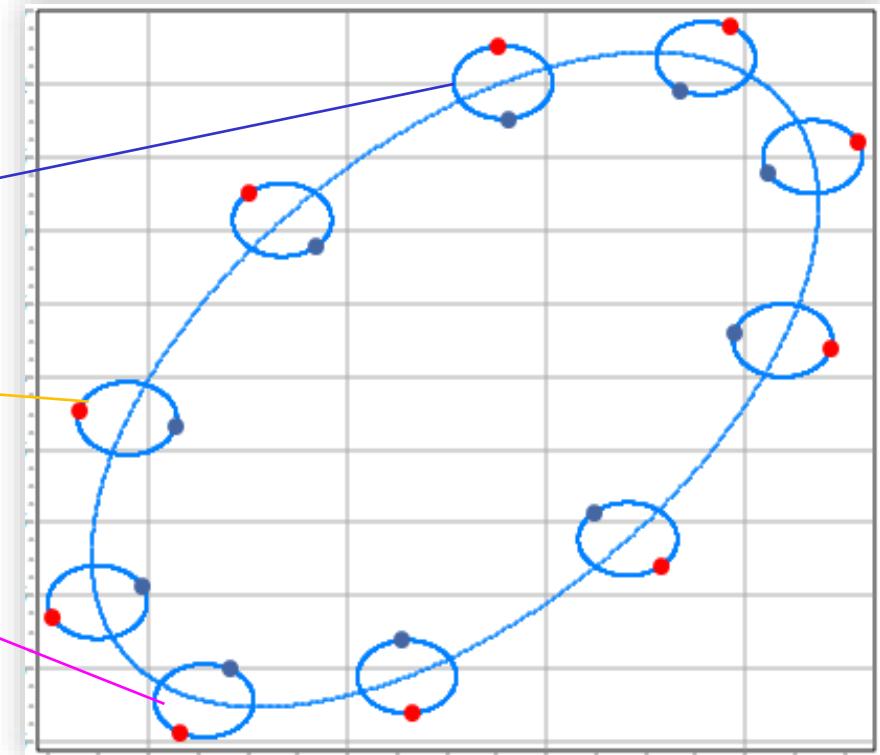
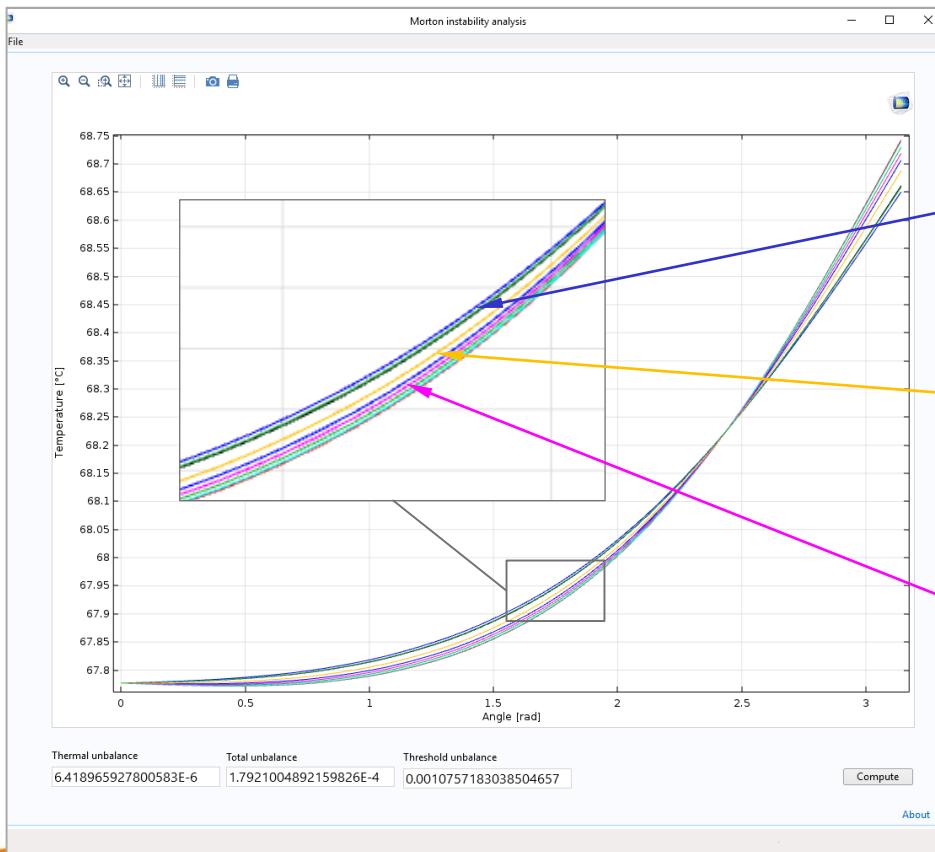
// model.result().numerical("gev1"). setResult();
double sol[][];
sol = model.result().numerical("gev1").getReal();
```



POLIBRIXIA

Innovation Engineering

4 – Comsol implementation



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Conclusion & future works

Implementation of a model to predict Morton effect (suggested by the literature)

- Hard numerical computation made by COMSOL
- A dedicated algorithm uses result computed with COMSOL

FUTURE WORKS

Eliminate approximation introduced to compute

- temperature distribution
- static equilibrium position

**Thank you for
your kind attention**