

# Electrowetting-on-dielectric Induced Droplet Actuation in $M \times N$ Array of Electrode



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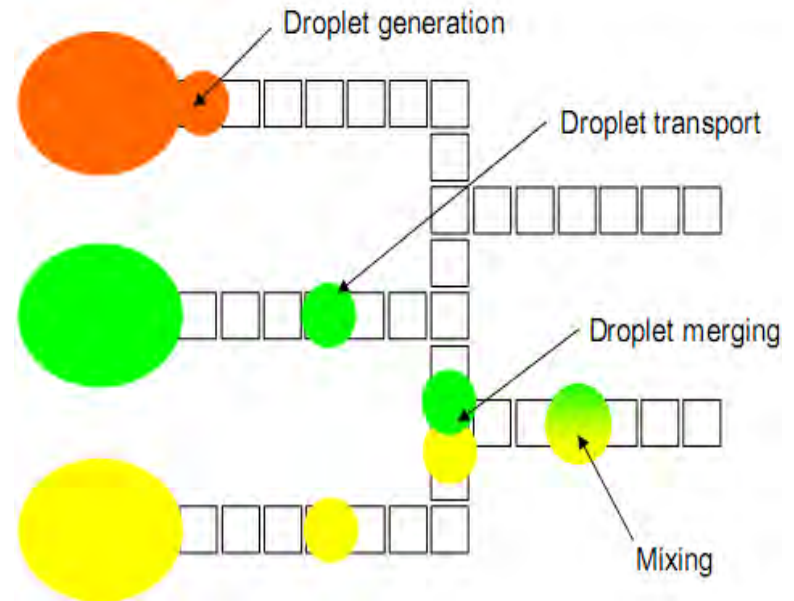
# Introduction

Droplet-based microfluidics (**Digital microfluidics**) is a new and emerging trend in microelectrofluidic systems (**MEFS**) and micro-total analysis systems ( **$\mu$ TAS**) in the past decade.

**Electrowetting-on-dielectric (EWOD)** is arguably the most flexible and powerful tool, used in many Lab-on-a-Chip (LoC) platforms .

## Advantages

- Small fluid volumes actuation
- Easy move, split, mix, and dispense operation
- Low power consumption
- Fast switching response
- No external pump
- Simple fabrication
- Low cost



## Application

- Liquid displays
- Liquid lenses
- Lab-on-a-chip
- Electrical switches
- Drug delivery
- Chip cooling

# EWOD Microsystems

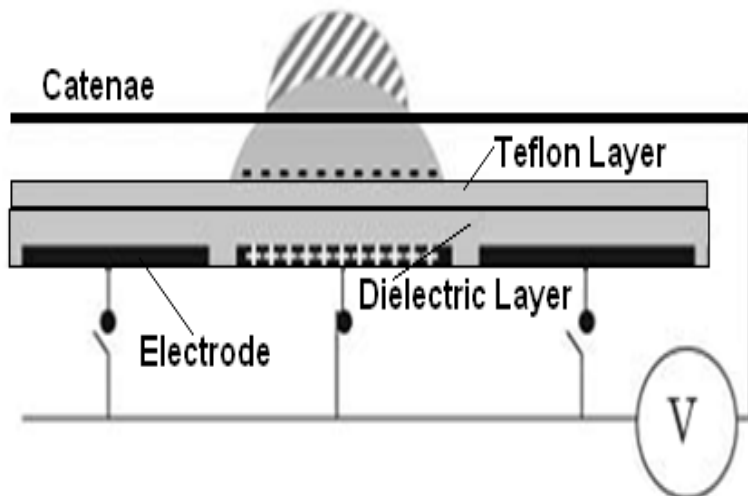


Figure 2a: With top catenae [1]

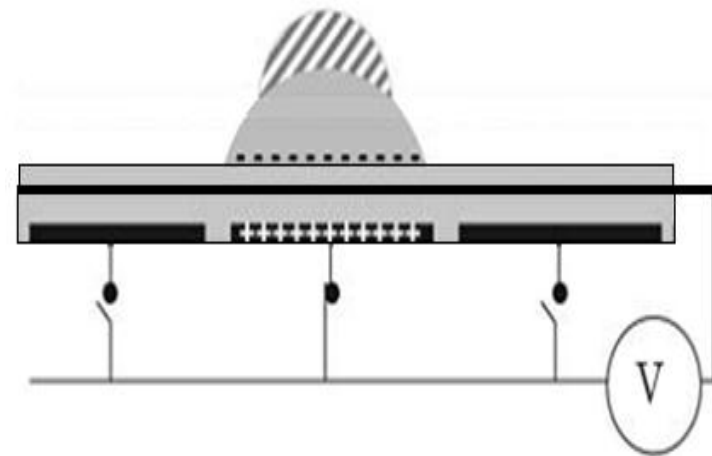


Figure 2b: With buried catenae [1]

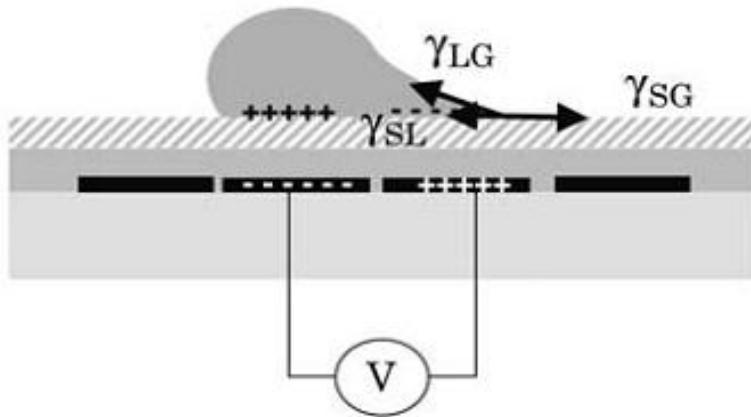


Figure 2c: Without catenae [1]

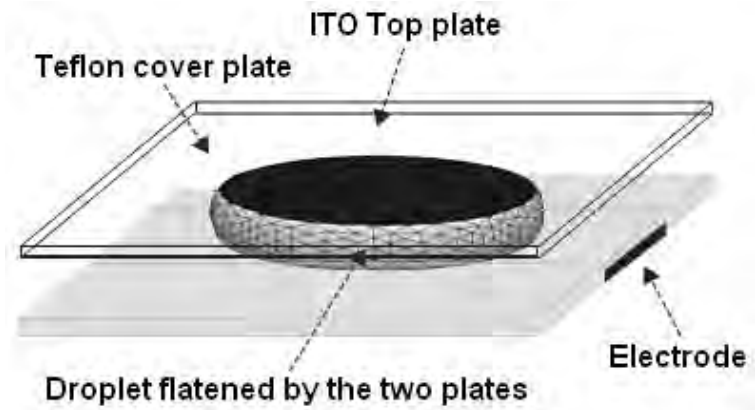


Figure 2d: Covered system [1]

# Addressing electrode in 3x3 or greater order matrix

- 1) Running conduction lines between the electrode gaps [2, 3]
  - Easy to fabricate and cost effective
  - Unwanted wetting of non electrode area
  - Limited to less order matrix
  
- 2) Multi-level metallization technique (IC fabrication) [2, 4]
  - Avoid parasitic unwanted wetting effect
  - Less number of bond pads and simple packaging
  - High fabrication cost and lengthy process step
  
- 3) Printed circuit board (PCB) technology [3, 5 and 6]
  - Low cost and flexible packaging
  - High actuation voltage
  - Temperature limitation
  
- 4) Cross-reference technique [7]
  - Single level metallization
  - Cartesian coordinate system
  - low cost and easy to fabricate

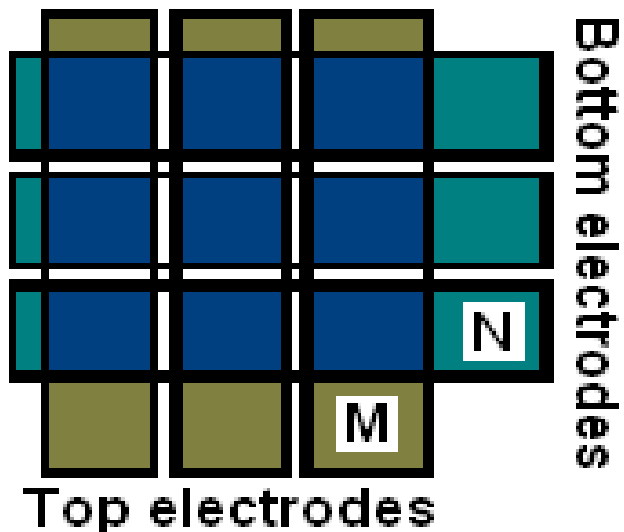
# Cross reference scheme

- Orthogonally aligned parallel electrodes in both top and bottom substrate.
- Row and column electrodes are energized with opposite signals.
- Cartesian coordinate system.

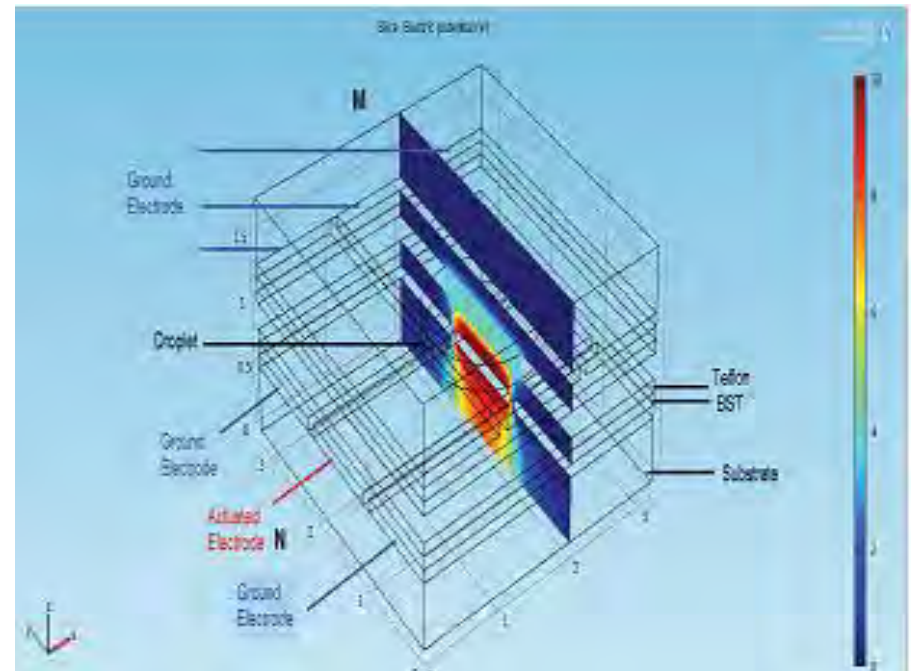
Initially at center (i.e. X-2, Y-2)

X-direction: (1, 2) or (3, 2)

Y-direction: (2, 1) or (2, 3)



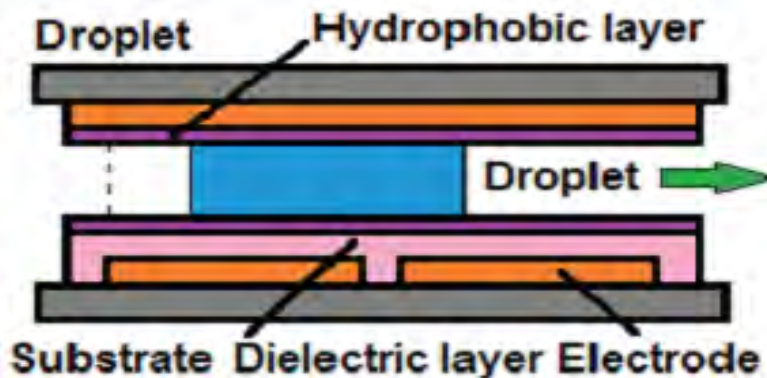
Top view of cross-reference design



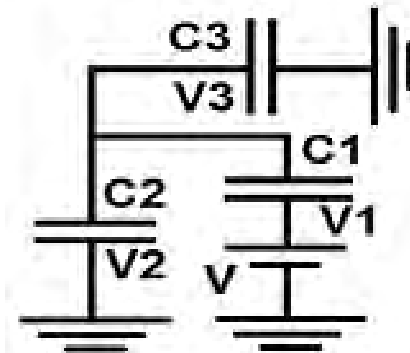
COMSOL setup

# Modeling of cross reference scheme

- Represented by a traditional covered two plate EWOD system.
- Three capacitors in electrical equivalent circuit.  
 $C1$  - between actuated electrode and droplet,  $C2$  - between non-actuated electrode and droplet and  $C3$  - between droplet and top ground electrode



Side view of droplet transition in cross reference scheme



Electrical equivalent circuit

- The energy gradient is the driving force according to energy-minimization model (Bahadur 2006 [8]).

# Modeling continues

- Droplet free energy is the sum of all the interfacial energy.

$$E(\mathbf{x}) = \gamma_{SL} \times A_1(\mathbf{x}) + \gamma_{SL} \times A_2(\mathbf{x}) + \gamma_{SL} \times A_3(\mathbf{x}) + \gamma_{LA} \times A_{SIDE} \quad (1)$$

Here  $\gamma_{SL}$ ,  $\gamma_{LA}$  and  $A_{SIDE}$  represent solid–liquid interfacial energy, liquid–air interfacial energy and cylindrical side around the droplet respectively.

- Reduction in interfacial tension is caused by the energy stored in capacitor.
- **Lippmann equation [14]** is used to quantify the decrease in solid–liquid interfacial energy .

$$\gamma_{SL}^V = \left( \gamma_{SL}^0 - \frac{k\epsilon_0 V^2}{2t} \right) \quad (2)$$

- Droplet free energy on actuation assuming liquid–air interfacial energy remain unchanged [15].

$$E(x) = \left( \gamma_{SL}^0 - \frac{k\epsilon_0 V_1^2}{2t} \right) \times A_1(x) + \left( \gamma_{SL}^0 - \frac{k\epsilon_0 V_2^2}{2t} \right) \times A_2(x) + \left( \gamma_{SL}^0 - \frac{k\epsilon_0 V_3^2}{2t} \right) \times A_3(x) + \gamma_{LA} \times A_{SIDE} \quad (3)$$



# Modeling continues

- Negative derivative of droplet free energy gives actuation force on droplet.

$$\begin{aligned} F(x) &= -\frac{dE(x)}{dx} = F_1(x) + F_2(x) + F_3(x) \\ F_1(x) &= \frac{k\varepsilon_0 V_1^2}{2t} \frac{dA_1(x)}{dx} + \frac{k\varepsilon_0 V_1 A_1(x)}{t} \frac{dV_1(x)}{dx} \\ F_2(x) &= \frac{k\varepsilon_0 V_2^2}{2t} \frac{dA_2(x)}{dx} + \frac{k\varepsilon_0 V_2 A_2(x)}{t} \frac{dV_2(x)}{dx} \\ F_3(x) &= \frac{k\varepsilon_0 V_3 A_3(x)}{t} \frac{dV_3(x)}{dx} \end{aligned} \quad (4)$$

- Actuation force has three components corresponding to the three regions of the droplet surface undergoing interfacial energy change.
- Results obtained from this model are identical to purely electromechanical model [8].
- Actuation force changes due to change in capacitance with droplet leading edge  $x$  varying from 0 to  $L$  (pitch length).

# COMSOL simulation

- Dimension:

- Top substrate-  $3.2 \text{ mm} \times 1 \text{ mm} \times 0.1 \text{ mm}$  ( along X-axis)
- Bottom substrate-  $3.2 \text{ mm} \times 1 \text{ mm} \times 0.1 \text{ mm}$  (along Y-axis)
- Electrode gap-  $0.1 \text{ mm}$
- Electrode area-  $1 \times 1 \text{ mm}$

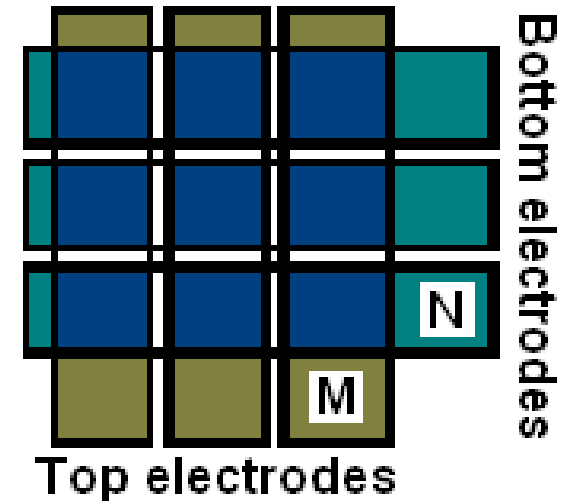
- Material property:

- BST (dielectric)-  $\epsilon_r=180$ , Thick- $0.1 \text{ mm}$
- Teflon (hydrophobic)-  $\epsilon_r=2.1$ , Thick- $0.1 \text{ mm}$

- Droplet is circular in shape (dia-  $L = 2r=1\text{mm}$ ) and move as a rigid body maintaining its circular shape.

- Boundary condition: (AC-DC Module)

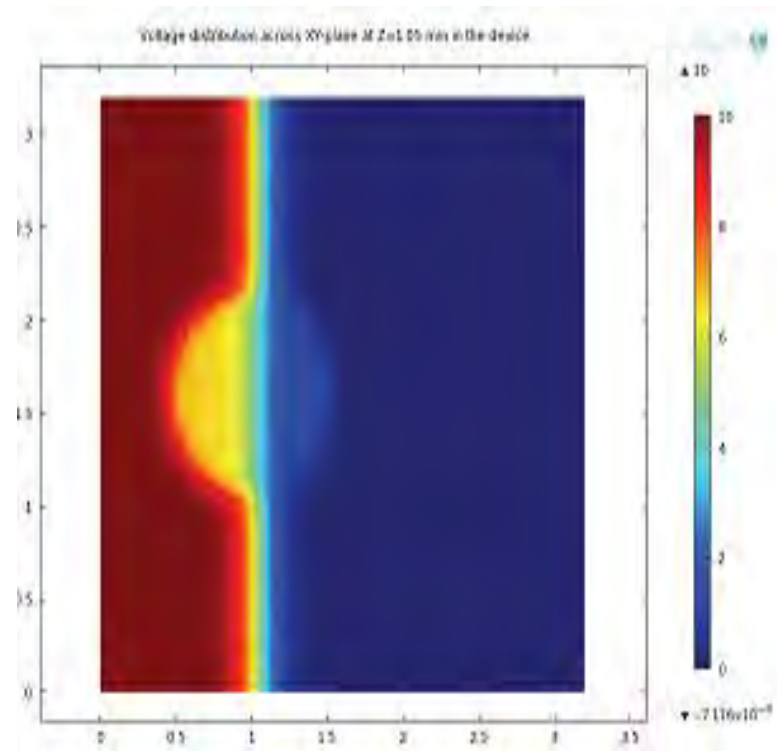
- Ground- all electrode except top first electrode
- Terminal (10V)- top first electrode



Top view of  
cross-reference design

# Simulation Result

- Voltage drop  $V_1$ ,  $V_2$  and  $V_3$  is calculated with droplet position ( $x$ )
- Droplet can be divided into two parts at a particular position ( $x$ )
  1. under the actuated electrode
  2. under un-actuated electrode
- These two parts have different potential.
- Voltage drops  $V_1$ ,  $V_2$  and  $V_3$  are calculated from 1D plot of two vertical 2D lines on XZ-plane
  - On actuated electrode
  - On un-actuated



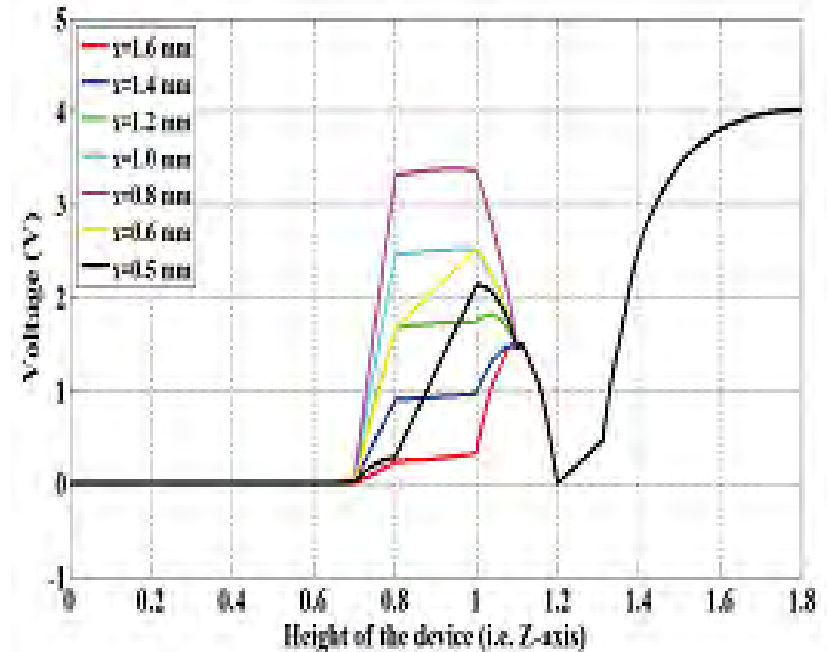
Voltage distribution across  
XY-plane at  $Z=1.05$  mm when  $x=1.0$

# Simulation Result

- Voltage distribution changes across capacitors during transition

- Step transition of 0.1 mm from  $x=1.6$  to 0.5 (i.e. complete transition from one electrode to the other) has been considered.

- Chopping the droplet and electrode assembly by a 2D ZX-plane.



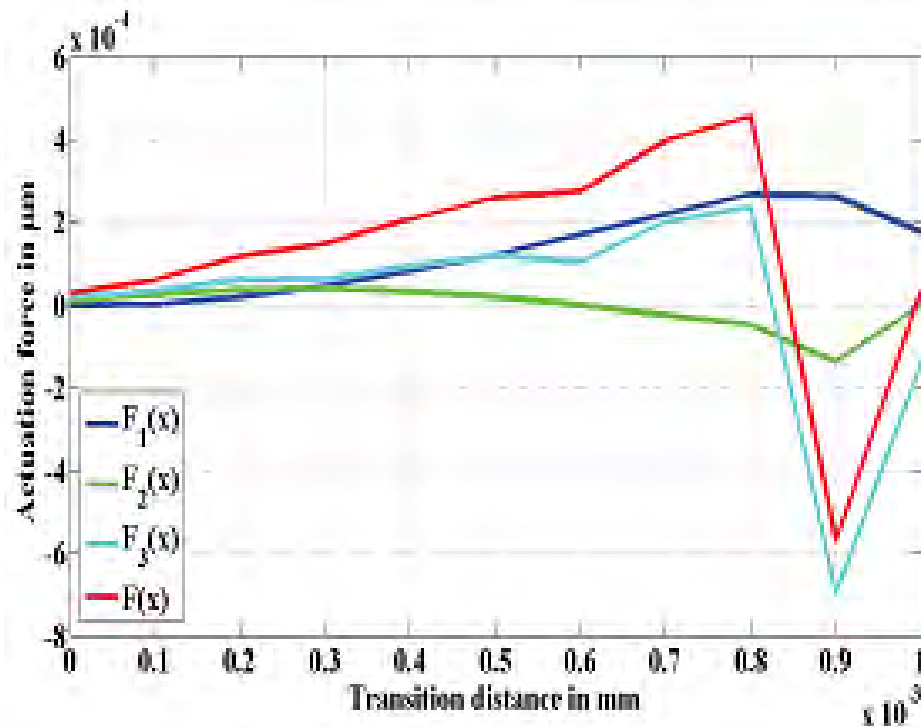
Voltage distribution along the height of the device (Z-axis) at  $x=0.5$  to 1.6 mm

# COMSOL Simulation

- Droplet moves from (2, 2) to (1, 2) electrode.
- Chopping by a 2D ZX-plane at  $Y=1.6$  mm. .
- Two vertical 2D lines on the XZ-plane.
  - Actuated electrode (point 1:  $X=0$ ,  $Y=1.15$  and point 2:  $X=1.8$ ,  $Y=1.15$  mm)
  - Un-actuated electrode (point 1:  $X=0$ ,  $Y=0.95$  and point 2:  $X=1.8$ ,  $Y=0.95$  mm).
- Voltage distribution 1D plot exported to MATLAB.
- Calculate potential difference (p.d.) across capacitors.
- Four interface points along the height (Z-axis) is used .
  - Interface point: 0.6, 0.8, 1.0 and 1.2.

# Simulation Result

- Procedure repeated for each step transition „x“ to calculate vector  $V1(x)$ ,  $V2(x)$  and  $V3(x)$ .
- Vector  $V1(x)$ ,  $V2(x)$  and  $V3(x)$  is applied to eqn. 4 to calculate actuation force through MATLAB program.



Actuation force during droplet transition from electrode to the other.

# Discussion

- The actuation force  $F(x)$  has three components  $F_1(x)$ ,  $F_2(x)$  and  $F_3(x)$
- These correspond to the three capacitors  $C_1$ ,  $C_2$  and  $C_3$  respectively responsible for interfacial energy change under the influence of the applied voltage.
- Net force is positive up to  $x=0.8$  mm, and it has positive slope as well.
- Beyond  $x=0.8$  mm, the slope and magnitude of  $F(x)$  becomes negative
- $F_3(x)$  is responsible for the negative slope of  $F(x)$  beyond  $x=0.8$ .
- This explains braking action to the droplet inertial moment. This helps the droplet finally stop at the actuated electrode and don't move beyond that.
- Undershoot in the  $F(x)$  is responsible for oscillatory motion in droplet before coming to rest.

# Conclusion

- The cross reference scheme is easy to fabricate and also does not compromise system performance.
- Adopt the Cartesian coordinate system .
- Equivalent electrical circuit remains same as two plate covered system.
- The force calculation using COMSOL Multiphysics gives better insight into EWOD dynamics without entrapping into long calculation to calculate voltage distribution vectors.
- It also explains braking action and oscillatory motion in the droplet before coming to rest.
- However, the simultaneous driving of multiple droplets in all possible combination in cross-referencing scheme is limited.



# References

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Thank You