Aggregation Kinetics of Colloidal Nanoparticles in a Circulating Microfluidic Cavity Meysam R. Barmi¹, Brian D. Piorek¹, Martin Moskovits², Carl D. Meinhart¹
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Introduction: Analyte contained in the air stream is absorbed into the cavity, mixes with the nanoparticles as a result of the circulating cavity flow. Therefore, the nanoparticles sequentially aggregate into clusters of higher orders which enables analyte detection using Raman spectroscopy.

Inlet: Air with Analyte **Results:** The dimer concentration is maximize to have an optimum analyte detection. The optimum point happens at:

$$\max\left(\frac{c_2}{c_{NP}}\right) at k c_{NP} t \approx 0.7$$

Conditions for numerical simulations:

- Ambient condition: $T_{\infty} = 20^{\circ}C$, $T_{w} = 10^{\circ}C$, RH = 50%
- Inlet velocity: $u_{in} = 10 \text{ mm/s}$,
- Analyte concentration: $c_a = 1 \ mM$

Physical phenomena:

- Fluid dynamics of the air flow
- Fluid dynamics of the microfluidic cavity
- Evaporation from air/liquid interface
- Absorption of the analyte from the interface
- Second order aggregation kinetics of nanoparticles

Goal:

 Optimum condition to get the highest number of the dimers in the cavity for efficient chemical detection

$$\nabla \cdot u_{g} = 0$$

$$\rho \left[\frac{\partial u_{g}}{\partial t} + (u_{g} \cdot \nabla) u_{g} \right] = -\nabla p_{g} + \nabla \cdot (\mu \nabla u_{g})$$

$$\frac{\partial c_{a}}{\partial t} + u_{g} \cdot \nabla c_{a} = \nabla \cdot (D_{a} \nabla c_{a})$$

$$\rho c \left(\frac{\partial T}{\partial t} + u_{g} \cdot \nabla T \right) = \nabla \cdot (k \nabla T)$$

$$\frac{\partial p_{v}}{\partial t} + u_{g} \cdot \nabla p_{v} = \nabla \cdot (D_{w} \nabla p_{v})$$

Aggregation rate equations: $\frac{k}{k_0} = e^{-V_{max}/k_BT} , V_{max} = \frac{V_0}{(1+\beta c_a)^{12/5}}$ $R_1 = -2kc_1c_1 - kc_2c_1 - kc_3c_1$ $R_2 = kc_1c_1 - kc_2c_1 - 2kc_2c_2$ $R_3 = kc_2c_1 - kc_3c_1$ $R_4 = kc_3c_1 + kc_2c_2$

- Initial concentration of nanoparticles: $c_{NP} = 100 \, pM$
- Aggregation kinetics: $k_0 = 10^8 [M^{-1} \text{s}^{-1}], V_0 = 3k_B T \text{ and } \beta = 10^4 [M^{-1}]$





Figure 1. Computational Domain and governing equations

Table 1. Multiphysics model

Physics	D	Variables	Domain

Figure 2. Formation of dimers in the cavity for c_{NP} = 100 pM



Figure 3. Formation of dimers in the cavity and air velocity vectors

Conclusions: We investigate the flow field, mass transport and aggregation kinetics to find the number of formed dimers according to the concentration of the analyte. There is an optimum point at $kc_{NP}t \approx 0.7$ where the number of formed

Weak form PDE: Initial curvature of the interface	1D	$oldsymbol{F}$	Interface
Deformed Geometry: Moving interface	2D	<i>X</i> , <i>Y</i>	Entire
Laminar Flow 1: Air flow in the microchannel	2D	u_g, v_g, p_g	Air
Laminar Flow 2: Liquid flow in the cavity	2D	u_w, v_w, p_w	Liquid
Heat Transfer: Temperature in the domain	2D	T	Entire
Transport of Diluted Species: Vapor pressure of water	2D	p_{ν}	Air
Weak form PDE: Concentration of analyte at the interface	1D	C _{BC}	Interface
Transport of Diluted Species: Analyte concentration in air	2D	C _a	Air
Transport of Diluted Species: Aggregation kinetics	2D	<i>C</i> _a , <i>C</i> ₁ , <i>C</i> ₂ , <i>C</i> ₃ , <i>C</i> ₄	Liquid

dimers is maxima for optimal chemical detection.

References:

- 1. Piorek, B., Lee, S., Santiago, J., Moskovits, M., Banerjee, S., Meinhart, M., Free-surface microfluidic control of surface-enhanced Raman spectroscopy for the optimized detection of airborne molecules, *Proceedings of the National Academy of Sciences*, **104**, 18898 (2007).
- 2. Moskovits, M.; Vlcková, B., Adsorbate-induced silver nanoparticle aggregation kinetics, *The Journal of Physical Chemistry B*, **109**, 14755–14758 (2005).
- 3. Hu, H., Larson, R., Evaporation of a sessile droplet on a substrate, *The Journal of Physical Chemistry B*, **106**, 1334–1344 (2002).
- 4. Girard, F., Antoni, M., Sefiane, K., On the effect of Marangoni flow on evaporation rates of heated water drops, *Langmuir*, **24**, 9207–9210 (2008).

Excerpt from the Proceedings of the 2012 COMSOL Conference in Boston